

```
In[1]:= SetDirectory["/www/user/fdahl/papers/Conjugation/"];
<< kappaLib.m
<< Petrov.m
```

KappaLib v1.1

Petrov routine loaded

### ■ Class I: (1bar(1) 1bar(1) 1bar(1))

$$\text{In[4]:= } \mathbf{B} = \begin{pmatrix} 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \end{pmatrix};$$

$$\text{In[5]:= } \mathbf{V} = \begin{pmatrix} \text{sigma1} & \text{tau1} & 0 & 0 & 0 & 0 \\ -\text{tau1} & \text{sigma1} & 0 & 0 & 0 & 0 \\ 0 & 0 & \text{sigma2} & \text{tau2} & 0 & 0 \\ 0 & 0 & -\text{tau2} & \text{sigma2} & 0 & 0 \\ 0 & 0 & 0 & 0 & \text{sigma3} & \text{tau3} \\ 0 & 0 & 0 & 0 & -\text{tau3} & \text{sigma3} \end{pmatrix};$$

```
In[6]:= Eigenvalues[V]
```

```
Out[6]= {sigma1 - i tau1, sigma1 + i tau1, sigma2 - i tau2,
sigma2 + i tau2, sigma3 - i tau3, sigma3 + i tau3}
```

### ■ mathcal(W) contains only one element:

$$\text{In[7]:= } \mathbf{W} = \begin{pmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 \end{pmatrix};$$

(\* Check that W has signature (+++---)\*)

```
Eigenvalues[W]
```

```
Out[8]= {-1, -1, -1, 1, 1, 1}
```

$$\text{In[9]:= } \mathbf{S} = \text{Sqrt}[2] \mathbf{B} \cdot \begin{pmatrix} \frac{1}{\sqrt{2}} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{\sqrt{2}} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{1}{\sqrt{2}} & 0 \\ 0 & \frac{1}{\sqrt{2}} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{\sqrt{2}} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{\sqrt{2}} \end{pmatrix};$$

### ■ Check that S is in set mathcal(S)

```
In[10]:= Transpose[S].B.S == W
```

```
Out[10]= True
```

**Compute result**

```
In[11]:= res = S.V.Inverse[S];
res // MatrixForm
```

```
Out[12]/MatrixForm=
```

$$\begin{pmatrix} \text{sigma1} & 0 & 0 & -\text{tau1} & 0 & 0 \\ 0 & \text{sigma2} & 0 & 0 & -\text{tau2} & 0 \\ 0 & 0 & \text{sigma3} & 0 & 0 & -\text{tau3} \\ \text{tau1} & 0 & 0 & \text{sigma1} & 0 & 0 \\ 0 & \text{tau2} & 0 & 0 & \text{sigma2} & 0 \\ 0 & 0 & \text{tau3} & 0 & 0 & \text{sigma3} \end{pmatrix}$$

```
In[13]:= Petrov[res]
```

```
Out[13]/MatrixForm=
```

$$\begin{pmatrix} -\text{tau1} & 0 & 0 & 0 & 0 & \text{sigma1} \\ 0 & -\text{tau2} & 0 & 0 & \text{sigma2} & 0 \\ 0 & 0 & -\text{tau3} & \text{sigma3} & 0 & 0 \\ 0 & 0 & \text{sigma3} & \text{tau3} & 0 & 0 \\ 0 & \text{sigma2} & 0 & 0 & \text{tau2} & 0 \\ \text{sigma1} & 0 & 0 & 0 & 0 & \text{tau1} \end{pmatrix}$$

- **Export notebook as .pdf**

```
In[14]:= NotebookPrint[SelectedNotebook[],
"/www/user/fdahl/papers/Conjugation/notebooks/ClassI.pdf"]
```