Yulia Mishura, Esko Valkeila: An extension of the Lévy characterization to fractional Brownian motion; Helsinki University of Technology, Institute of Mathematics, Research Reports A514 (2006).

**Abstract:** Assume that X is a continuous square integrable process with zero mean defined on some probability space  $(\Omega, F, P)$ . The classical characterization due to P. Lévy says that X is a Brownian motion if and only if X and  $X_t^2 - t$ ,  $t \ge 0$  are martingales with respect to the intrinsic filtration  $\mathbb{F}^X$ . We extend this result to fractional Brownian motion.

## AMS subject classifications: 60G15,60E05,60H99

Keywords: fractional Brownian motion, Lévy theorem

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